

LEZIONE 10
Espressioni contenenti monomi

$$\begin{aligned}
 & \left[\left(-\frac{5}{3} a^4 b x^2 \right) : \left(-\frac{10}{3} a^4 x^2 \right) - \frac{1}{16} b^6 : \left(-\frac{1}{32} b^5 \right) \right] : \left[-\frac{1}{8} a^{12} b^6 x^3 : \left(\frac{3}{4} a^{12} b^5 x^3 \right) \right] = \\
 & = \left[\frac{\cancel{5}^1}{\cancel{3}_1} \cdot \frac{\cancel{3}^1}{2} b + \frac{1}{16} \cdot \frac{\cancel{32}^2}{1} b \right] : \left[\frac{\cancel{1}^1}{8} \cdot \frac{\cancel{4}^1}{3} b \right] = \\
 & = \left[\frac{1}{2} b + \frac{2}{1} b \right] : \left[\frac{1}{6} b \right] = \left[\frac{1+4}{2} b \right] : \left[\frac{1}{6} b \right] = \\
 & = \left[\frac{5}{2} b \right] : \left[\frac{1}{6} b \right] = \frac{5}{\cancel{2}^1} \cdot \frac{\cancel{6}^3}{1} = \textcircled{15}
 \end{aligned}$$

$$\begin{aligned}
& \left[\left(-\frac{13}{2}ab + \frac{5}{1}ab \right)^3 \cdot \left(\frac{13}{2}ab - \frac{5}{1}ab \right)^2 \cdot \left(-\frac{3}{2}ab \right)^4 \right] \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \left(\frac{3a-b}{2} \right)^3 \\
= & \left[\left(\frac{-13ab + 10ab}{2} \right)^3 \cdot \left(\frac{13ab - 10ab}{2} \right)^2 \cdot \left(-\frac{3}{2}ab \right)^4 \right] \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \left(\frac{3a-b}{2} \right)^3 \\
= & \left[\left(-\frac{3}{2}ab \right)^3 \cdot \left(\frac{3}{2}ab \right)^2 \cdot \left(-\frac{3}{2}ab \right)^4 \right] \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \left(\frac{3a-b}{2} \right)^3 \\
= & \left[-\left(\frac{3}{2}ab \right)^3 \cdot \left(\frac{3}{2}ab \right)^2 \cdot \left(\frac{3}{2}ab \right)^4 \right] \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \frac{25a^2}{4} = \\
= & \left[-\left(\frac{3}{2}ab \right)^5 \cdot \left(\frac{3}{2}ab \right)^4 \right] \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \frac{25a^2}{4} = \\
= & -\left(\frac{3}{2}ab \right) \cdot \left(-\frac{1}{2}ab \right) \cdot b^2 \cdot \frac{25a^2}{4} = \\
= & \frac{3}{4}a^2b^2 - \frac{25}{4}a^2b^2 = \frac{3 - 25}{4}a^2b^2 = -\frac{22}{4}a^2b^2 \\
& \quad \quad \quad = \boxed{-\frac{11}{2}a^2b^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{3} b \cdot (a^3 b)^2 + \left(\frac{2}{3} x y\right)^3 \cdot (a^2 m)^3 + \frac{2}{5} a^3 \left(\frac{1}{3} a b\right)^3 + \frac{1}{3} a m^3 x^3 y (a y)^5 = \\
& = \frac{1}{3} b \cdot a^6 b^2 + \frac{8}{27} x^3 y^3 \cdot a^6 m^3 + \frac{2}{5} a^3 \left(\frac{1}{27} a^3 b^3\right) + \frac{1}{3} a m^3 x^3 y \cdot a^5 y^5 = \\
& = \frac{1}{3} a^6 b^3 + \frac{8}{27} a^6 m^3 x^3 y^3 + \frac{2}{135} a^6 b^3 + \frac{1}{3} a^6 m^3 x^3 y^6 = \\
& = \left(\frac{1}{3} + \frac{2}{135}\right) a^6 b^3 + \left(\frac{8}{27} + \frac{1}{3}\right) a^6 m^3 x^3 y^6 = \\
& = \frac{(45+2)}{135} a^6 b^3 + \frac{(8+9)}{27} a^6 m^3 x^3 y^6 = \\
& = \boxed{\frac{47}{135} a^6 b^3 + \frac{17}{27} a^6 m^3 x^3 y^6} \quad \boxed{\frac{47 a^6 b^3 + 85 a^6 m^3 x^3 y^6}{135}}
\end{aligned}$$

$$\begin{aligned}
& -2xy \left(-\frac{1}{3}x^2y\right)^2 : (-6x^3y) - \left\{ \left[-x^2(-y)^2 \right]^2 \right\}^2 : \left(-\frac{2}{3}x^2y\right)^3 - \frac{1}{3}x^2y^2 = \\
& = -2xy \cdot \left(\frac{1}{9}x^4y^2\right) : (-6x^3y) - \left\{ \left[-x^2y^2 \right]^2 \right\}^2 : \left(-\frac{2}{3}x^2y\right)^3 - \frac{1}{3}x^2y^2 = \\
& = -\frac{2}{9}x^5y^3 : (-6x^3y) - \left\{ \left[x^4y^4 \right]^2 \right\} : \left(-\frac{2}{3}x^2y\right)^3 - \frac{1}{3}x^2y^2 = \\
& = \frac{2}{9} \cdot \frac{1}{81} x^2y^2 - \frac{x^8y^8}{9} \cdot \left(-\frac{2}{3}x^2y\right)^3 - \frac{1}{3}x^2y^2 = \\
& = \frac{1}{27}x^2y^2 + \frac{8}{27}x^2y^2 - \frac{1}{3}x^2y^2 = \\
& = \frac{1}{27}x^2y^2 + \frac{8}{27}x^2y^2 - \frac{1}{3}x^2y^2 = \frac{1}{27}x^2y^2 - \frac{1}{3}x^2y^2 = \\
& = \frac{1}{3}x^2y^2 - \frac{1}{3}x^2y^2 = 0
\end{aligned}$$