

$$\frac{1}{a} a^2 = \frac{a^2}{a}$$

Lezione 15
Espressioni polinomiali

$$\begin{aligned}
 &= \frac{1}{6} \left(\frac{a}{3} + \frac{b}{2} \right) - \frac{2}{3} b \left(\frac{a}{4} + \frac{3}{2} a \right) - \left(\frac{1}{3} a^2 - \frac{2}{3} b^2 - \frac{11}{6} ab \right) \cdot \frac{1}{2} = \\
 &= \frac{a}{6} + \frac{ab}{4} - \frac{2}{12} ab - \frac{1}{2} ab - \left(\frac{1}{6} a^2 - \frac{2}{3} b^2 - \frac{11}{12} ab \right) = \\
 &= \frac{1}{6} a + \frac{1}{4} ab - \frac{1}{6} ab - \frac{1}{2} ab - \frac{1}{6} a^2 + \frac{1}{3} b^2 + \frac{11}{12} ab = \\
 &= \left(\frac{1}{4} - \frac{1}{6} - 1 + \frac{11}{12} \right) ab + \frac{1}{3} b^2 = \left(\frac{3 - 2 - 12 + 11}{12} \right) ab + \frac{1}{3} b^2 = \\
 &= \boxed{\frac{1}{3} b^2}
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\left[\left(\frac{1}{2}x + y \right) \left(\frac{y}{3} - x \right)^2 + \frac{4}{3}xy \right] \cdot \left(\frac{2}{3}y^2 + x^2 \right) + \left(\frac{5}{3}y^4 + x^4 + \frac{1}{3}x^2y \right)} \\
&= \sqrt{\left[\left(\frac{1}{6}xy - \frac{1}{2}x^2 + \frac{1}{3}y^2 - xy \right)^2 + \frac{4}{3}xy \right] \cdot \left(\frac{2}{3}y^2 + x^2 \right) + \left(\frac{5}{3}y^4 + x^4 + \frac{1}{3}x^2y \right)} \\
&= \sqrt{\left[\frac{1}{6}xy - \frac{1}{2}x^2 + \frac{2}{3}y^2 - 2xy + \frac{4}{3}xy \right] \cdot \left(\frac{2}{3}y^2 + x^2 \right) + \frac{5}{3}y^4 + x^4 + \frac{1}{3}x^2y} \\
&= \sqrt{\left[\left(\frac{1}{3} - 2 + \frac{4}{3} \right)xy - x^2 + \frac{2}{3}y^2 \right] \cdot \left(\frac{2}{3}y^2 + x^2 \right) + \frac{5}{3}y^4 + x^4 + \frac{1}{3}x^2y} \\
&= \sqrt{\left[\left(\frac{1-6+4}{3} \right)xy - x^2 + \frac{2}{3}y^2 \right] \cdot \left(\frac{2}{3}y^2 + x^2 \right) + \frac{5}{3}y^4 + x^4 + \frac{1}{3}x^2y}
\end{aligned}$$

$$\begin{aligned}
&= \left\{ \left[-\frac{1}{3}xy - x^2 + \frac{2}{3}y^2 \right] \left(\frac{2}{3}y^2 + x^2 \right) + \frac{5}{9}y^4 + x^4 + \frac{1}{3}x^3y \right\} : (-2y^3) \\
&= \left\{ \cancel{\frac{2}{9}xy^3} - \frac{2}{9}xy^3 - \frac{1}{3}x^3 - \frac{2}{3}x^2y^2 - x^4 + \frac{4}{9}y^4 + \frac{2}{3}xy^2 + \frac{5}{9}y^4 + \frac{1}{3}x^3y \right\} : (-2y^3) \\
&= \left\{ -\frac{2}{9}xy^3 + y^4 \right\} : (-2y^3) = \\
&= \cancel{\frac{2}{9}} \cdot \frac{1}{2} x + \frac{1}{2} y = \boxed{\frac{1}{9}x - \frac{1}{2}y}
\end{aligned}$$

$$\frac{z}{x} \cdot 82 = 4 \quad \frac{4}{x} \cdot 82 = 8$$

$$\begin{aligned}
 & \left\{ \left[\left(x + \frac{1}{2}y \right) \left(b + \frac{2}{3}a \right) - bx - \frac{1}{3}ay \right] (ax - 2by) \cdot 6 + 5by(ax + by) \right\} \cdot \left(-\frac{1}{2} \right)^2 = 2 \\
 & = \left\{ \left[\cancel{bx} + \frac{2}{3}ax + \frac{1}{2}by + \frac{1}{3}ay - \cancel{bx} - \frac{1}{3}ay \right] (ax - 2by) \cdot 6 + 5abxy + 5b^2y^2 \right\} \cdot \left(-\frac{1}{2} \right)^2 \\
 & = \left\{ \left(\frac{2}{3}ax + \frac{1}{2}by \right) (ax - 2by) \cdot 6 + 5abxy + 5b^2y^2 \right\} \cdot \frac{1}{4} = \\
 & = \left\{ \left(\frac{2}{3}ax^2 - \frac{4}{3}abxy + \frac{1}{2}abxy - b^2y^2 \right) \cdot 6 + 5abxy + 5b^2y^2 \right\} \cdot \frac{1}{4} = \\
 & = \left\{ 4a^2x^2 - \cancel{8abxy} + \cancel{3abxy} - \cancel{6b^2y^2} + \cancel{5abxy} + \cancel{5b^2y^2} \right\} \cdot \frac{1}{4} = \\
 & = \left\{ 4a^2x^2 - b^2y^2 \right\} \cdot \frac{1}{4} = \\
 & = \left\{ 4a^2x^2 - b^2y^2 \right\} \cdot \frac{1}{4} = \\
 & = \boxed{16a^2x^2 - 4b^2y^2}
 \end{aligned}$$

$$\begin{aligned}
& 2 \left(a^3 + \frac{1}{4} \right) \left(\frac{1}{16} - a^3 \right) + \left[\left(a - \frac{1}{2} \right) \left(a^4 + \frac{1}{2} a^3 + \frac{1}{4} a^2 \right) \cdot \left(a^2 + \frac{1}{8} \right) \right] : \left(\frac{1}{2} a^2 \right) \\
&= \left(2a^3 + \frac{1}{2} \right) \left(\frac{1}{16} - a^3 \right) + \left[\left(a^5 + \frac{1}{2} a^4 + \frac{1}{4} a^3 - \frac{1}{2} a^4 - \frac{1}{4} a^3 - \frac{1}{8} a^2 \right) \left(a^2 + \frac{1}{8} \right) \right] : \left(\frac{1}{2} a^2 \right) \\
&= \left(\frac{1}{8} a^3 - 2a^6 + \frac{1}{32} - \frac{1}{2} a^3 \right) + \left[\left(a^5 - \frac{1}{8} a^2 \right) \left(a^2 + \frac{1}{8} \right) \right] : \left(\frac{1}{2} a^2 \right) = \\
&= \frac{1}{8} a^3 - 2a^6 + \frac{1}{32} - \frac{1}{2} a^3 + \left[a^8 + \frac{1}{8} a^5 - \frac{1}{8} a^5 - \frac{1}{64} a^2 \right] : \left(\frac{1}{2} a^2 \right) = \\
&= \frac{1}{8} a^3 - 2a^6 + \frac{1}{32} - \frac{1}{2} a^3 + \left[a^8 - \frac{1}{64} a^2 \right] : \frac{1}{2} a^2 = \frac{3}{8} a^6 \\
&= \frac{1}{8} a^3 - 2a^6 + \frac{1}{32} - \frac{1}{2} a^3 + 2a^6 - \frac{1}{32} = \left(\frac{1}{8} - \frac{1}{2} \right) a^3 - \left(\frac{1}{8} - \frac{1}{8} \right) a^6 \uparrow
\end{aligned}$$