

LEZIONE 4
ESPRESSIONI CON I NUMERI RELATIVI

$$\begin{aligned} & [-2^2]^{-5} \cdot 8^{-3} \cdot 4^5 \cdot [(-2)^2]^3 \cdot (-2)^3 = \\ & = [-4]^{-5} \cdot 8^{-3} \cdot 4^5 \cdot [4]^3 \cdot (-8) = \\ & = \left[-\frac{1}{4}\right]^5 \cdot \left(\frac{1}{8}\right)^3 \cdot 4^5 \cdot 4^3 \cdot (-8) = \\ & = \left[-\frac{1}{2^2}\right]^5 \cdot \left(\frac{1}{2^3}\right)^3 \cdot (2^2)^5 \cdot (2^2)^3 \cdot (-1) \cdot 2^3 = \\ & = \frac{1}{2^{10}} \cdot \frac{1}{2^9} \cdot 2^{10} \cdot 2^6 \cdot (-1) \cdot 2^3 = \frac{1}{2^1} = 1 \end{aligned}$$

$$4 = 2 \cdot 2 = 2^2$$

$$8 = 2 \cdot 2 \cdot 2 = 2^3$$

$$\begin{aligned}
& \left\{ 2^{-2} \cdot 2^3 : 2^2 \cdot [(2^5 \cdot 2)^{-2} : (2^3 \cdot 2)^{-1}] \right\}^{-1} : 2^2 = \\
& = \left\{ 2^{-2} \cdot 2^3 : 2^2 \cdot [(2^6)^{-2} : (2^4)^{-1}] \right\}^{-1} : 2^2 = \\
& = \left\{ 2^{-2} \cdot 2^3 : 2^2 \cdot [2^{-12} : 2^{-4}] \right\}^{-1} : 2^2 = \\
& = \left\{ 2^{-2} \cdot 2^3 : 2^2 \cdot 2^{-8} \right\}^{-1} : 2^2 = \\
& = \left\{ 2^1 : 2^2 \cdot 2^{-8} \right\}^{-1} : 2^2 = \left\{ 2^{-1} \cdot 2^{-8} \right\}^{-1} : 2^2 = \left\{ 2^{-9} \right\}^{-1} : 2^2 = 2^9 : 2^2 = \sqrt{\boxed{2^7}}
\end{aligned}$$

$$\begin{aligned}
& -12 - (-4) = \\
& = -12 + 4 = -8 \\
& -1 + (-8) = -9
\end{aligned}$$

$$\begin{aligned}
& -12 : 3 + 4 + \{ 5 - (-2)^3 - [4 - (1 + 2 \cdot 4 - 6) : (-3) + 5] - 6 + 2 \} = \\
& = -12 : 3 + 4 + \{ 5 - (-8) - [4 - (1 + 8 - 6) : (-3) + 5] - 6 + 2 \} = \\
& = -12 : 3 + 4 + \{ 5 - (-8) - [4 - 3 : (-3) + 5] - 6 + 2 \} = \\
& = -12 : 3 + 4 + \{ 5 - (-8) - [4 + 1 + 5] - 6 + 2 \} = \quad \overbrace{\quad\quad}^0 \quad \overbrace{\quad\quad}^3 \\
& = -12 : 3 + 4 + \{ 5 + 8 - 10 - 6 + 2 \} = \\
& = \cancel{-4} + \cancel{4} + \{ -1 \} = \boxed{-1}
\end{aligned}$$

$$\begin{aligned}
& \left[-\frac{1}{4} : \left(-\frac{3}{8} - \frac{1}{2}\right)\right] : \left[\left(\frac{3}{2} - \frac{3}{4}\right) : \frac{1}{2} - \left(-\frac{1}{4} + \frac{1}{8}\right) : \left(-\frac{1}{4}\right)\right] = \\
& = \left[-\frac{1}{4} : \left(\frac{-3-4}{8}\right)\right] : \left[\left(\frac{6-3}{4}\right) : \frac{1}{2} - \left(\frac{-2+1}{8}\right) : \left(-\frac{1}{4}\right)\right] = \\
& = \left[-\frac{1}{4} : \left(-\frac{7}{8}\right)\right] : \left[\frac{3}{4} : \frac{1}{2} - \left(-\frac{1}{8}\right) : \left(-\frac{1}{4}\right)\right] = \\
& = \left[\frac{1}{\cancel{4}} \cdot \frac{8}{7}\right] : \left[\frac{3}{\cancel{4} \cdot 2} \cdot \frac{2}{1} - \frac{1}{\cancel{8}} \cdot \frac{1}{1}\right] = \\
& = \frac{2}{7} : \left[\frac{3}{2} - \frac{1}{2}\right] = \frac{2}{7} : \frac{2}{2} = \frac{2}{7} : 1 = \frac{2}{7} \cdot 1 = \boxed{\frac{2}{7}}
\end{aligned}$$

$$\begin{aligned}
& \left[\left(-3 + \frac{5}{2}\right) \cdot \frac{12}{7} + \frac{14}{22} : \frac{21}{11} \right] \cdot \frac{21}{22} : \left(\frac{2}{5} - \frac{2}{3}\right) = \\
& = \left[\left(\frac{-6+5}{2}\right) \cdot \frac{12}{7} + \frac{\cancel{2}^1 \cancel{14}^1}{\cancel{22}^1 \cancel{11}^1} \right] \cdot \frac{21}{22} : \left(\frac{6-10}{15}\right) = \\
& = \left[-\frac{1}{2} \cdot \frac{12}{7} + \frac{1}{3} \right] \cdot \frac{21}{22} : \left(-\frac{4}{15}\right) = \\
& = \left[-\frac{6}{7} + \frac{1}{3} \right] \cdot \frac{21}{22} : \left(-\frac{4}{15}\right) = \\
& = \left[\frac{-18+7}{21} \right] \cdot \frac{21}{22} : \left(-\frac{4}{15}\right) = -\frac{\cancel{21}^1}{\cancel{21}^1} \cdot \frac{\cancel{21}^1}{\cancel{22}^1} : \left(-\frac{4}{15}\right) = \\
& = \left(-\frac{1}{2}\right) : \left(-\frac{4}{15}\right) = \frac{1}{2} \cdot \frac{15}{4} = \left(\frac{15}{8}\right) \checkmark
\end{aligned}$$

$$\begin{aligned}
& \left[\frac{3}{5} : \left(\frac{4}{1} + \frac{8}{5} \right) \cdot \left(\frac{2}{5} + \frac{1}{1} \right) - \frac{6}{5} : (-8) \right] \cdot \left\{ \frac{5}{3} + \left[\left(-\frac{2}{7} + \frac{3}{4} \right) : \left(\frac{1}{2} - \frac{1}{3} \right) \right] \cdot \left(\frac{1}{4} - \frac{7}{15} \right) \right\} \\
&= \left[\frac{3}{5} : \left(\frac{20+8}{5} \right) \cdot \left(\frac{2+5}{5} \right) + \frac{3}{5} \cdot \frac{1}{8} \right] \cdot \left\{ \frac{5}{3} + \left[\left(\frac{-8+3}{4} \right) : \left(\frac{3-2}{6} \right) \right] \cdot \left(\frac{15-7}{15} \right) \right\} \\
&= \left[\frac{3}{5} : \frac{28}{5} \cdot \frac{7}{5} + \frac{3}{20} \right] \cdot \left\{ \frac{5}{3} + \left[\left(-\frac{5}{4} \right) : \frac{1}{6} \right] \cdot \frac{8}{15} \right\} = \\
&= \left[\frac{3}{5} \cdot \frac{8}{28} \cdot \frac{7}{5} + \frac{3}{20} \right] \cdot \left\{ \frac{5}{3} + \left[-\frac{5}{4} \cdot \frac{8}{6} \right] \cdot \frac{8}{15} \right\} = \\
&= \left[\frac{3}{20} + \frac{3}{20} \right] \cdot \left\{ \frac{5}{3} + \left(-\frac{15}{4} \right) \cdot \frac{8}{15} \right\} = \\
&= \frac{3}{10} \cdot \left\{ \frac{5}{3} - 4 \right\} = \frac{3}{10} \cdot \left\{ \frac{5-12}{3} \right\} = \frac{3}{10} \cdot \left(-\frac{7}{3} \right) = \left(-\frac{7}{10} \right) \checkmark
\end{aligned}$$