

Lezione 25

$$\begin{aligned}
 & 5x^2 - 2xy - 16y^2 \\
 &= \underbrace{5x^2}_{\text{}} - \underbrace{2y}_{\text{}}x - \underbrace{16y^2}_{\text{}} = \\
 &= \underbrace{5x^2 + 8yx}_{\text{}} - \underbrace{10yx - 16y^2}_{\text{}} = \\
 &= x(5x + 8y) - 2y(5x + 8y) = \\
 &= \underline{(5x + 8y)(x - 2y)}
 \end{aligned}$$

$$\begin{aligned}
 s &= -2y \\
 p &= -80y^2
 \end{aligned}$$

y	·	80y
2y	·	40y
4y	·	10y
5y	·	16y
8y	·	10y

(8y) + (-10y)

$$\begin{aligned}
& 4a^2 - 11ab + 7b^2 \\
&= 4a^2 - \underbrace{11ba} + \underbrace{7b^2} = \\
&= \underbrace{4a^2 - 4ba} - \underbrace{7ba + 7b^2} = \\
&= 4a(a-b) - 7b(a-b) = \\
&= \underline{(a-b)(4a-7b)}
\end{aligned}$$

$$S = -11b$$

$$P = 28b^2$$

$b \cdot 28b$
$2b \cdot 14b$
$4b \cdot 7b$

$-4b$	$-7b$
-------	-------

$$\begin{aligned}
 x^4 + 4x^2 - 45 &= \\
 &= t^2 + 4t - 45 \\
 &= (t + 9)(t - 5) = \\
 &= (t - 5)(t + 9) = \\
 &= (x^2 - 5)(x^2 + 9) = \\
 &= (x + \sqrt{5})(x - \sqrt{5})(x^2 + 9)
 \end{aligned}$$

$$\boxed{x^2 = t}$$

$$\begin{array}{l}
 p = -45 \\
 \hline
 s = 4 \\
 \hline
 r = -5 \quad r + 9
 \end{array}$$

1 · 45
3 · 15
5 · 9

Divisione polinomiale

$$(x^2 + x + 1) : (x + 1) = ? \text{?} \text{?}$$

quoziente resto

$$7 : 2 = 3 \text{ r } 1$$

$$7 = 2 \cdot 3 + 1$$

DIVIDENDO      DIVISORE

Algoritmo della divisione numerica

$$a = b \cdot q + r$$

DIVIDENDO      DIVISORE      QUOZIENTE      RESTO

$$A(x) = B(x) \cdot Q(x) + R(x)$$

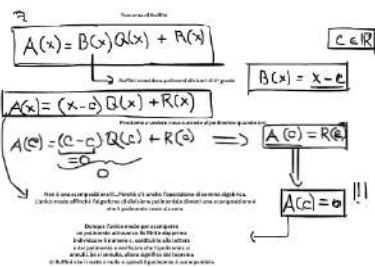
POLIN. DIVIDENDO      POLIN. DIVISORE      POLINOMIO QUOZIENTE      POLINOMIO RESTO

Algoritmo della divisione polinomiale

Sempre utilizzabile

$$\begin{array}{r}
 6a^2 + 5a + 1 \\
 - 6a^2 - 6a \\
 \hline
 // \quad -a + 1 \\
 \quad + a + 1 \\
 \hline
 // \quad 2
 \end{array}
 \quad
 \begin{array}{r}
 a + 1 \\
 \hline
 6a - 1
 \end{array}
 \quad
 \begin{array}{r}
 2 \\
 \hline
 2
 \end{array}$$

$$\begin{aligned}
 6a^2 + 5a + 1 &= (a+1)(6a-1) + 2 = \\
 &= 6a^2 - a + 6a - 1 + 2 = \\
 &= 6a^2 + 5a + 1 \quad \checkmark
 \end{aligned}$$



$A(x) = x^3 - 5x^2 - 4x + 20$

$A(1) = 1 - 5 - 4 + 20 = 12 \neq 0$   
 $A(-1) = -1 - 5 + 4 + 20 = 18 \neq 0$   
 $A(2) = 8 - 20 - 8 + 20 = 0$  ✓

$c = 2$

$A(x) = B(x)Q(x)$        $B(x) = (x - c) = (x - 2)$

$$x^3 - 5x^2 - 4x + 20 = (x - 2)Q(x)$$

$x^3 - 5x^2 - 4x + 20$	$  x - 2$	
$-x^2 + 2x^2$	$-2x + 4$	
$-3x^2 - 4x + 20$	$+3x - 6$	
$+10x + 20$	$-10x + 20$	
$0$	$0$	

$Q(x) = x^2 - 3x + 10$

$x^3 - 5x^2 - 4x + 20 = (x - 2)(x^2 - 3x + 10) = (x - 2)(x + 2)(x - 5)$

$x^2 - 3x + 10 =$   
 $(x + 2)(x - 5) = (x + 2)(x - 5)$

$p = 10$   
 $q = -3$   
 $1 \cdot 10$   
 $2 \cdot 5$        $\alpha = 2$   
 $\beta = -5$

$$A(x) = 3x^3 + 2x^2 - 4x - 3$$

$$D_3 = \{\pm 1, \pm 3\}$$

$$A(1) = 3 + 2 - 4 - 3 = -2 \neq 0$$

$$A(-1) = -3 + 2 + 4 - 3 = 0$$

$$c = -1$$

$$B(x) = x - c = x - (-1) = (x + 1)$$

	3	2	-4	-3
-1		-3	1	3
	3	-1	-3	0

$$3x^3 + 2x^2 - 4x - 3 = (x + 2)(3x^2 - 10x - 3)$$

$$3x^2 - 10x - 3$$

$$\begin{array}{l} p = -9 \\ s = -1 \end{array}$$

$$\begin{array}{l} 1 \cdot 9 \\ 3 \cdot 3 \end{array}$$

Non è scomponibile in Q

Nei reali, in R, posso usare il discriminante di un polinomio di secondo grado (da vedere in seguito...)