

Lezione 46

$$\frac{m^6 - n^6}{(a^2 - b^2)} = \frac{(m^3 - n^3)(m^3 + n^3)}{(a - b)(a + b)}$$

$$\frac{m^3 - n^3}{(a - b)(a + b)} = \frac{(m - n)(m^2 + mn + n^2)}{(a - b)(a + b)}$$

$$\frac{m^3 + n^3}{(a - b)(a + b)} = \frac{(m + n)(m^2 - mn + n^2)}{(a - b)(a + b)}$$

$$m^6 - n^6 = (m - n)(m^2 + mn + n^2)(m + n)(m^2 - mn + n^2) =$$

$$= (m - n)(m + n)(m^2 + mn + n^2)(m^2 - mn + n^2)$$

$$\boxed{25 - \frac{x^2}{9} = \left(5 - \frac{x}{3}\right)\left(5 + \frac{x}{3}\right)}$$

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

$$(a - b)(a^2 + ab + b^2) =$$

$$= a^3 + a^2b + ab^2 - ab^2 - b^3 =$$

$$= a^3 - b^3$$

$$\frac{2a^3b^3 - a^4 - a^2b^6}{a^2} = \frac{2ab^3 - a^2 - b^6}{1} \leftarrow \text{RACCOLIMENTO TOTALE}$$

$$= a^2 \left[ -1(b^6 + a^2 - 2ab^3) \right] =$$

$$= -a^2 \left( \frac{b^6 + a^2 - 2ab^3}{1} \right) \leftarrow \text{QUADRATO DI BINOMIO}$$

$$= -a^2 (b^3 - a)^2$$

$$x^{10} + x^9 + x^8 + x^7 =$$

$$= x^7 (x^3 + x^2 + x + 1) \leftarrow \text{RACC. TOTALE}$$

$$= x^7 [x^2(x+1) + 1(x+1)] \leftarrow \text{RACC. PARZIALE}$$

$$= x^7 \cdot [(x+1)(x^2+1)] = x^7 (x+1)(x^2+1)$$

$$\begin{aligned}
 & \boxed{m^2 - (n + fm)^2} = \text{DIFF. 01} \\
 & \underbrace{m^2}_{A^2} - \underbrace{(n + fm)^2}_{B^2} = (A-B)(A+B) \quad \text{QUADR. GENERALIZZATI} \\
 & = \left[ \underbrace{m}_{A} - \underbrace{(n + fm)}_B \right] \left[ \underbrace{m}_{A} + \underbrace{(n + fm)}_B \right] = \boxed{A^2 - B^2} \\
 & = (m - n - fm) (m + n + fm)
 \end{aligned}$$